

Principles of Computer Science II

Abstract Data Types

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Lecture 15



Heap Data Structures

Heap is a special case of balanced binary tree data structure where the root-node key is compared with its children and arranged accordingly.

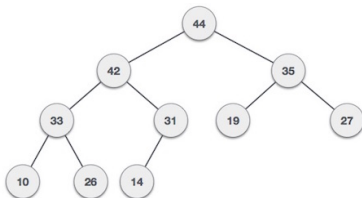
If α has child node β then

$$\text{key}(\alpha) \geq \text{key}(\beta)$$

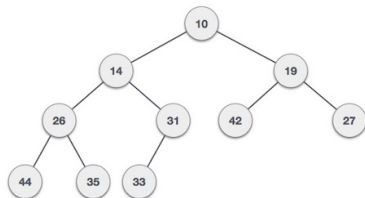
- ▶ As the value of parent is greater than that of child, this property generates **Max Heap**.
- ▶ By changing the criterion we can also get a **Min Heap**.



Max Heap



Min Heap



Max Heap – Add

1. Create a new node at the end of heap.
2. Assign new value to the node.
3. Compare the value of this child node with its parent.
4. If value of parent is less than child, then swap them.
5. Repeat step 3 & 4 until Heap property holds.

Note – In Min Heap construction algorithm, we expect the value of the parent node to be less than that of the child node.



Max Heap – Add Example

Input 35 33 42 10 14 19 27 44 26 31



Max Heap – Add Example

Input **35** 33 42 10 14 19 27 44 26 31

35



Max Heap – Add Example

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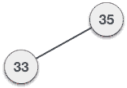
Max Heap – Add Example

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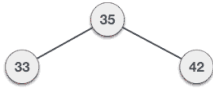
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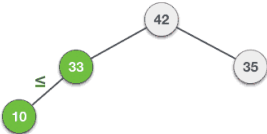
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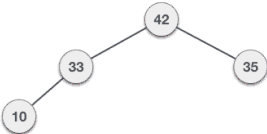
Max Heap – Add Example

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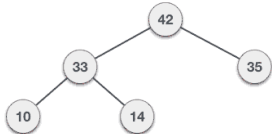
Max Heap – Add Example

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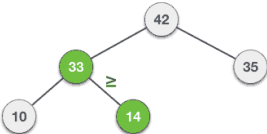
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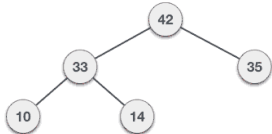
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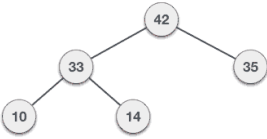
Max Heap – Add Example

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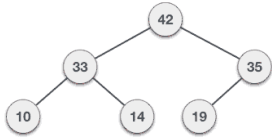
Max Heap – Add Example

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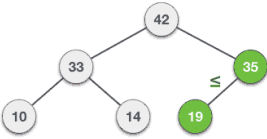
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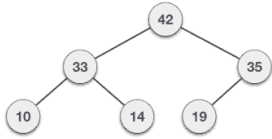
Max Heap – Add Example

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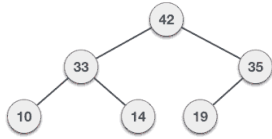
Max Heap – Add Example

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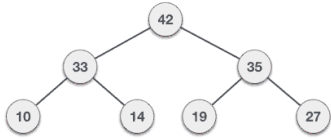
Max Heap – Add Example

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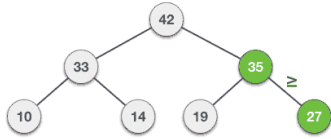
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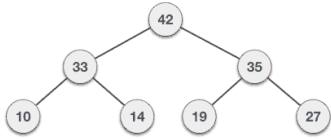
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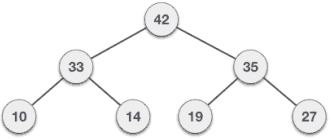
Max Heap – Add Example

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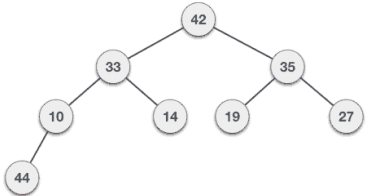
Max Heap – Add Example

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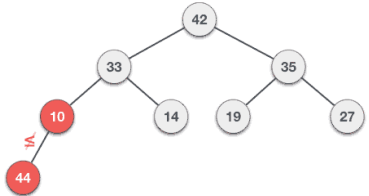
Max Heap – Add Example

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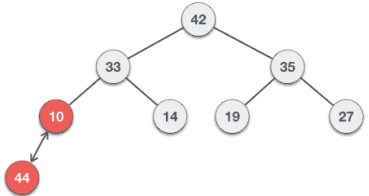
Max Heap – Add Example

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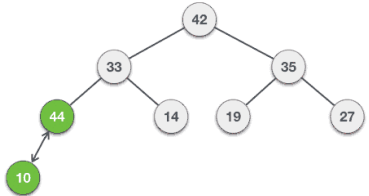
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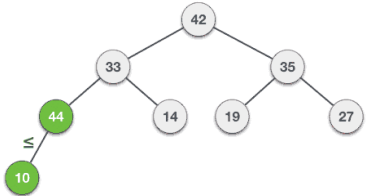
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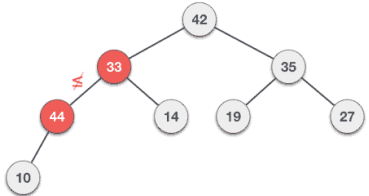
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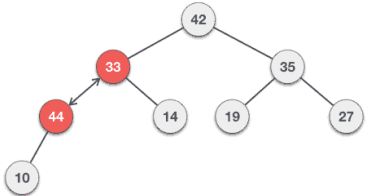
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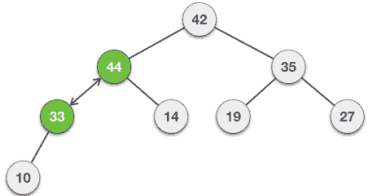
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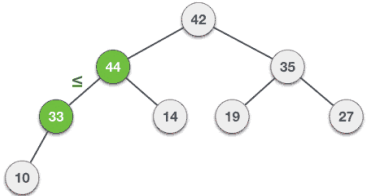
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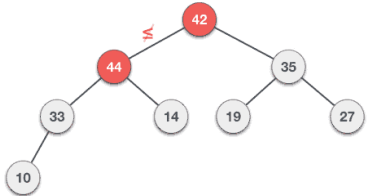
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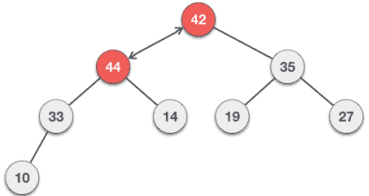
Max Heap – Add Example

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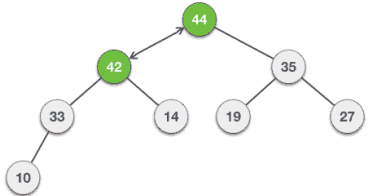
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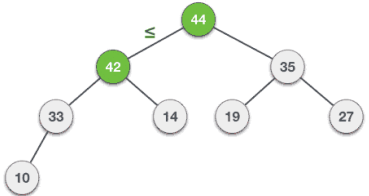
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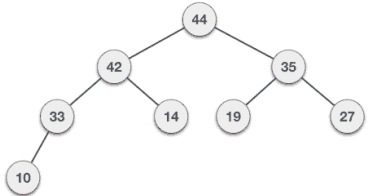
Max Heap – Add Example

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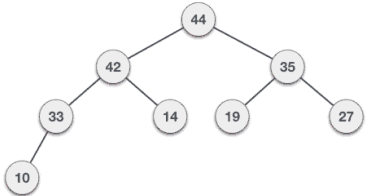
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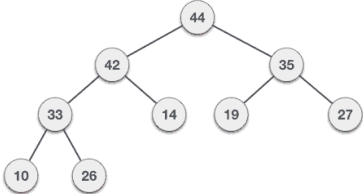
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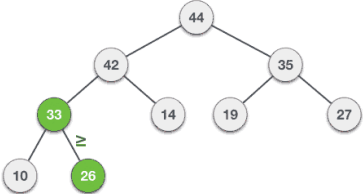
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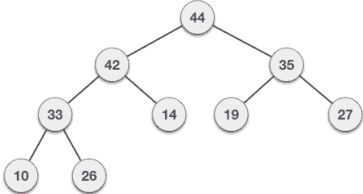
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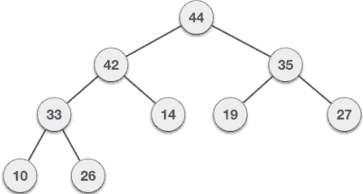
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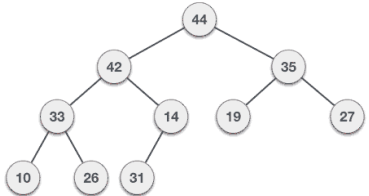
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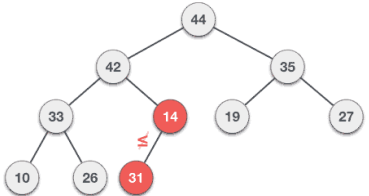
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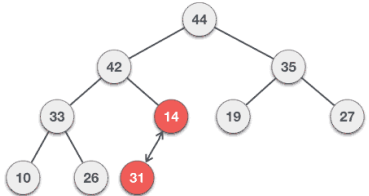
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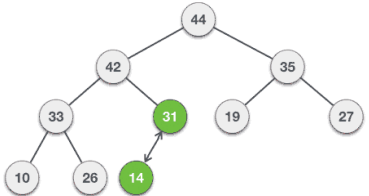
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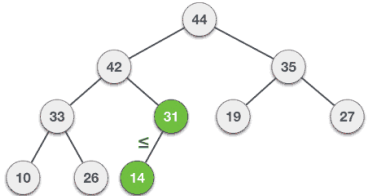
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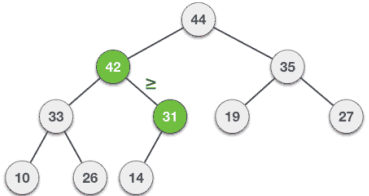
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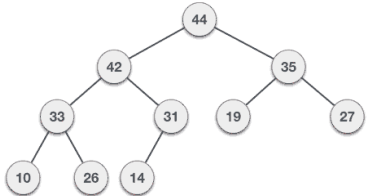
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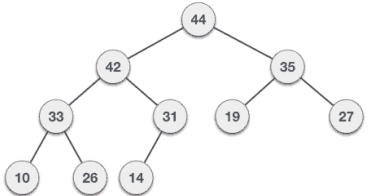
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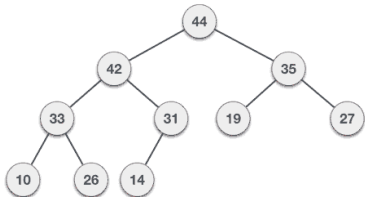
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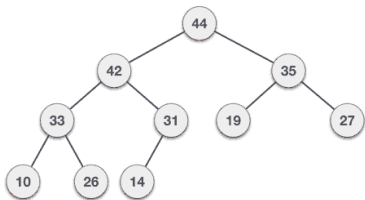


Max Heap – Deletion

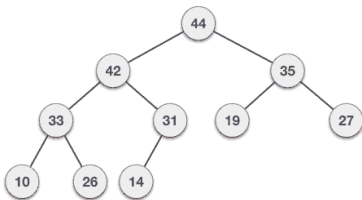
1. Remove root node.
2. Move the last element of last level to root.
3. Compare the value of this child node with its parent.
4. If value of parent is less than child, then swap them.
5. Repeat step 3 & 4 until Heap property holds.



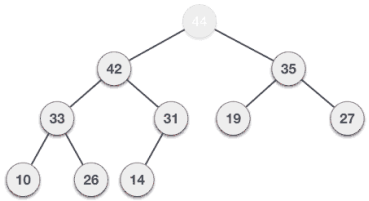
Max Heap – Deletion Example



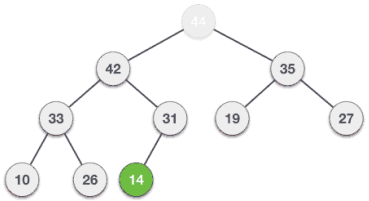
Max Heap – Deletion Example



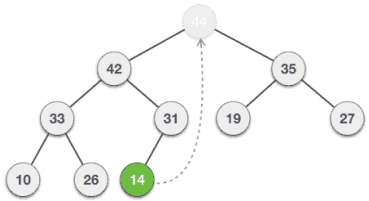
Max Heap – Deletion Example



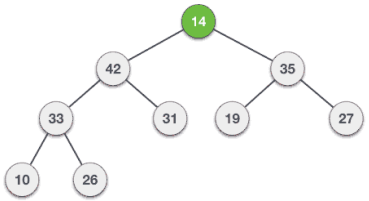
Max Heap – Deletion Example



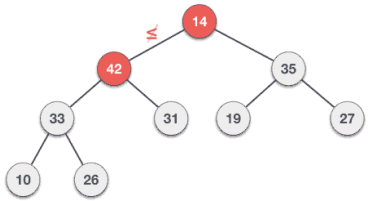
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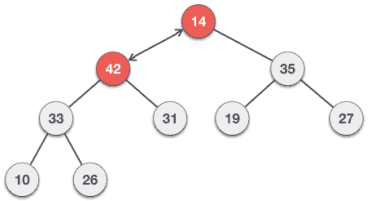
Max Heap – Deletion Example



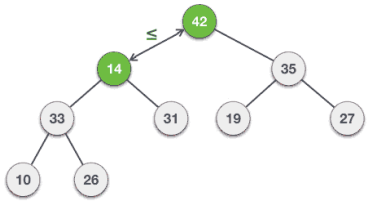
Max Heap – Deletion Example



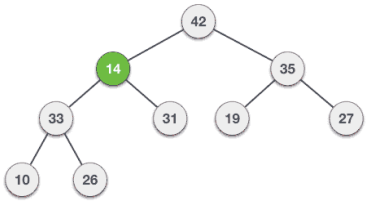
Max Heap – Deletion Example



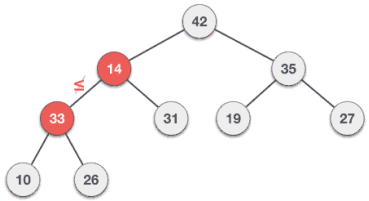
Max Heap – Deletion Example



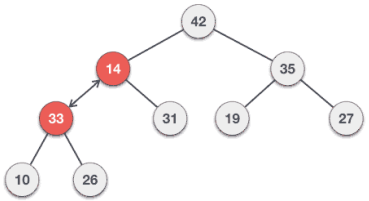
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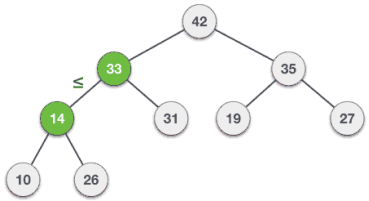
Max Heap – Deletion Example



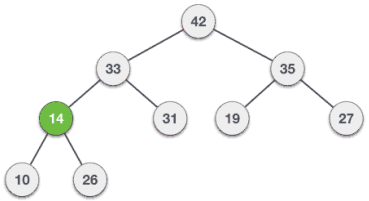
Max Heap – Deletion Example



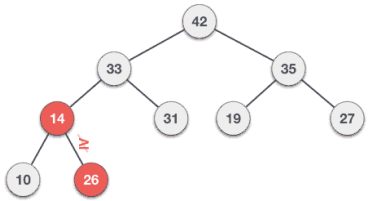
Max Heap – Deletion Example



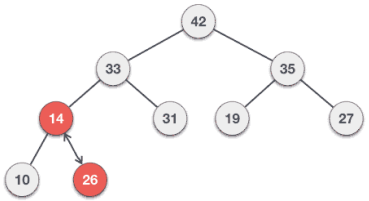
Max Heap – Deletion Example



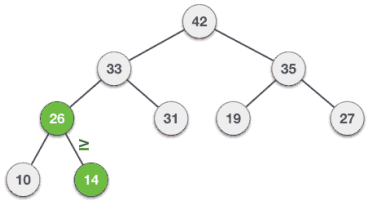
Max Heap – Deletion Example



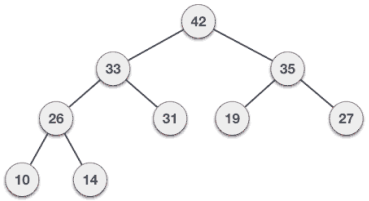
Max Heap – Deletion Example



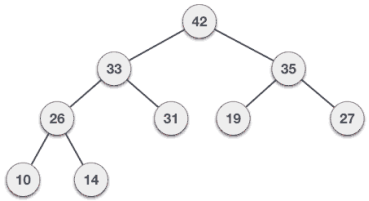
Max Heap – Deletion Example



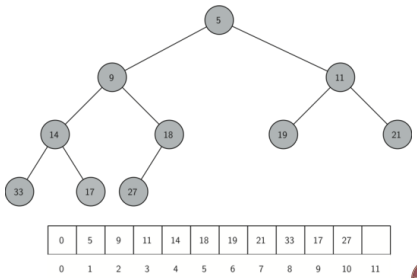
Max Heap – Deletion Example



Max Heap – Deletion Example



Heap Implementation using Arrays



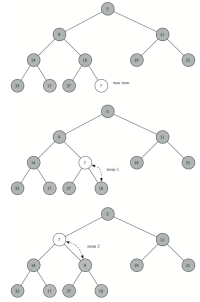
Binary Heap

```

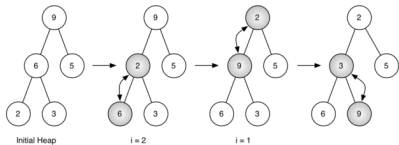
class BinHeap:
    def __init__(self):
        self.heapList = [0]
        self.currentSize = 0
    
```



Binary Heap – Insertion



Binary Heap – Build from List



Binary Heap – Build from List

```
def buildHeap(self,alist):  
    i = len(alist) // 2  
    self.currentSize = len(alist)  
    self.heapList = [0] + alist[:]  
    while (i > 0):  
        self.percDown(i)  
        i = i - 1
```

4th Assignment

- ▶ <https://www.rosalind.info/>
 - ▶ Complete the following **challenges**:
dna, rna, revc, gc, subs, cons, lcs, revp, splc, lexf, fib, lgis
 - ▶ <http://rosalind.info/problems/{challenge}>
- ▶ Create a GitHub repository and upload the code for each exercise.
- ▶ Email ichatz@diag.uniroma1.it
Subject: [PCS2] Homework 4
A link with your GitHub repository, with your solutions, for all challenges.
Also send your user account link:
<http://rosalind.info/users/{username}>
- ▶ **Deadline: 4/December/2020, 23:59**