

# Principles of Computer Science II

## Algorithms for Bioinformatics

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Lecture 3



## Pebble Game



- ▶ Game played in turns by 2 players.
- ▶ Two piles of equal number of pebbles.
- ▶ Each turn a player may either
  - ▶ take 1 pebble **from a single pile**, or
  - ▶ take 1 pebble **from both piles**.
- ▶ The player that takes the last pebble wins.



## Best Strategy for Winning the Pebble Game

- ▶ Does the first player always have an advantage?
- ▶ Let's consider the most simplified version.
  - ▶ Pebbles = 2 – we call this the  $2 \times 2$  game.
  - ▶ Is there a winning strategy?
  - ▶ What is the winning strategy?



## Generalized Strategy for Winning the Pebble Game

- ▶ Can we generalize the strategy of the  $2 \times 2$  game?
- ▶ What about the  $3 \times 3$  game?
  - ▶ Consider different game sequences.
- ▶ Consider the  $n \times n$  game.
  - ▶ Is there only one winning strategy?
  - ▶ How easy it is to describe our strategy?
  - ▶ Quality of solution.



We build a matrix for all game combinations. Four actions:

1.  $\uparrow$  take one pebble from pile A.
2.  $\leftarrow$  take one pebble from pile B.
3.  $\swarrow$  take one pebble from each pile.
4. \* ignore game.

	0	1	2	3	4	5	6	7	8	9	10
0											
1											
2											
3											
4											
5											
6											
7											
8											
9											
10											



- ▶ The first player always loses the  $2 \times 2$ .
- ▶ Clearly also for  $0 \times 2, 0 \times 4, \dots$
- ▶ Can we generalize for all games where each pile has an even number of pebbles?

	0	1	2	3	4	5	6	7	8	9	10
0	*		*		*		*		*		*
1											
2	*		*								
3											
4	*										
5											
6	*										
7											
8	*										
9											
10	*										



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	0	1	2	3	4	5	6	7	8	9	10
0	*		*		*		*		*		*
1											
2	*		*		*		*		*		*
3											
4	*		*		*		*		*		*
5											
6	*		*		*		*		*		*
7											
8	*		*		*		*		*		*
9											
10	*		*		*		*		*		*



- ▶ Only 1 option for all  $0 \times 1, 0 \times 3, \dots$  and  $1 \times 0, 3 \times 0, \dots$

	0	1	2	3	4	5	6	7	8	9	10
0	*		*		*		*		*		*
1											
2	*		*		*		*		*		*
3											
4	*		*		*		*		*		*
5											
6	*		*		*		*		*		*
7											
8	*		*		*		*		*		*
9											
10	*		*		*		*		*		*



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	0	1	2	3	4	5	6	7	8	9	10
0	*	←	*	←	*	←	*	←	*	←	*
1	↑										
2	*		*		*		*		*		*
3	↑										
4	*		*		*		*		*		*
5	↑										
6	*		*		*		*		*		*
7	↑										
8	*		*		*		*		*		*
9	↑										
10	*		*		*		*		*		*



- ▶ Only 1 option for all  $0 \times 1, 0 \times 3, \dots$  and  $1 \times 0, 3 \times 0, \dots$
- ▶ Can we generalize for other columns/rows where one pile has an odd number of pebbles and the other an even?

	0	1	2	3	4	5	6	7	8	9	10
0	*	←	*	←	*	←	*	←	*	←	*
1	↑		↑		↑		↑		↑		↑
2	*	←	*	←	*	←	*	←	*	←	*
3	↑		↑		↑		↑		↑		↑
4	*	←	*	←	*	←	*	←	*	←	*
5	↑		↑		↑		↑		↑		↑
6	*	←	*	←	*	←	*	←	*	←	*
7	↑		↑		↑		↑		↑		↑
8	*	←	*	←	*	←	*	←	*	←	*
9	↑		↑		↑		↑		↑		↑
10	*	←	*	←	*	←	*	←	*	←	*



- ▶ Only 1 option for all  $0 \times 1, 0 \times 3, \dots$  and  $1 \times 0, 3 \times 0, \dots$
- ▶ Can we generalize for other columns/rows where one pile has an odd number of pebbles and the other an even?
- ▶ What about the other rows/columns?

	0	1	2	3	4	5	6	7	8	9	10
0	*	←	*	←	*	←	*	←	*	←	*
1	↑	↘	↑	↘	↑	↘	↑	↘	↑	↘	↑
2	*	←	*	←	*	←	*	←	*	←	*
3	↑	↘	↑	↘	↑	↘	↑	↘	↑	↘	↑
4	*	←	*	←	*	←	*	←	*	←	*
5	↑	↘	↑	↘	↑	↘	↑	↘	↑	↘	↑
6	*	←	*	←	*	←	*	←	*	←	*
7	↑	↘	↑	↘	↑	↘	↑	↘	↑	↘	↑
8	*	←	*	←	*	←	*	←	*	←	*
9	↑	↘	↑	↘	↑	↘	↑	↘	↑	↘	↑
10	*	←	*	←	*	←	*	←	*	←	*



## An algorithmic approach for winning the Pebble Game

- ▶ How can we build the matrix for any game size, e.g.,  $20 \times 20$
- ▶ What is the algorithm for winning the game?



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- ▶ How can we build the matrix for any game size, e.g.,  $20 \times 20$
- ▶ What is the algorithm for winning the game?
- ▶ Why should I care?



## An algorithmic approach for winning the Pebble Game

- ▶ How can we build the matrix for any game size, e.g.,  $20 \times 20$
- ▶ What is the algorithm for winning the game?
- ▶ Why should I care?
- ▶ It is the **sequence alignment** problem.
- ▶ The computational idea used to solve both problems is the same.
- ▶ We need to understand how algorithms work.



## Methodology of solving a computational problem

- ▶ What is the problem at hand ?
  - ▶ Identify & Understand assumptions.
  - ▶ What is our goal ?
  - ▶ Identify similar problems/solutions in the bibliography
  - ▶ What are the theoretical foundation ?
  - ▶ Can we formulate the problem in a unambiguous and precise way ?
- ▶ What is the Input that we have ?
  - ▶ Do we have enough data or should we try to collect?
  - ▶ Open data sets ?
  - ▶ Can we synthesize input data ?
- ▶ What is the expected Output ?



## Solution Sketch

- ▶ Do we have a rough idea of a solution ?
- ▶ Do we have identified an approach to solving the problem ?
  - ▶ think again !
  - ▶ go through the definition – maybe we overlooked something ?
- ▶ Write down a **solution sketch**
  - ▶ check if it adheres to the initial assumptions
  - ▶ can you try it out with a small input ?
- ▶ Is the solution correct ? can we provide some arguments ?
- ▶ What is the performance of the solution ?
- ▶ Can we think of a more efficient solution ?



## Implement the first version

- ▶ Pick your programming language of choice.
- ▶ Implement your solution
  - ▶ No need to try to make it elegant / fast.
  - ▶ Remember Donald Knuth: There is no such thing as early optimization.
- ▶ Get some input data
  - ▶ Open datasets
  - ▶ Small size
- ▶ Limited Evaluation
  - ▶ does it work ?
  - ▶ do you need to make any modifications ?
  - ▶ are there special cases that you missed ?

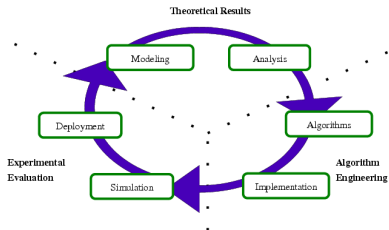


## Iterative approach

- ▶ Step-by-step development
  - ▶ Continuous development.
  - ▶ Agile methodology.
- ▶ Identify issues in previous version
  - ▶ Code beautification.
  - ▶ Bug fixes.
  - ▶ Performance improvements.
  - ▶ Additional functionalities.
- ▶ Implement improvements
  - ▶ Make sure code is always clean + easy to maintain.
  - ▶ Keep detailed records of changes.
  - ▶ Always keep history of source code evolution.
- ▶ Performance Evaluation
  - ▶ bigger input.
  - ▶ scalability ?



## Theoretical – Practical Approach Cycle



## Quality of Code

John Woods

Always code as if the guy who ends up maintaining your code will be a violent psychopath who knows where you live.

