Principles of Computer Science II Sorting Algorithms

Ioannis Chatzigiannakis

Sapienza University of Rome

Lecture 5

Selection Sort Algorithm

exchanges it with the element in the first position, then find the second smallest element and exchange it with the element in the second position, and continues in this way until the entire array is sorted.

101100102121212

1011/0011/01/05 05 000

This algorithm first finds the smallest element in the array and



1011/01/12/12/12 2:00

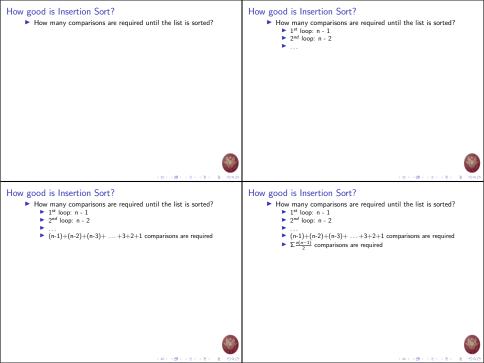
Selection Sort: Example

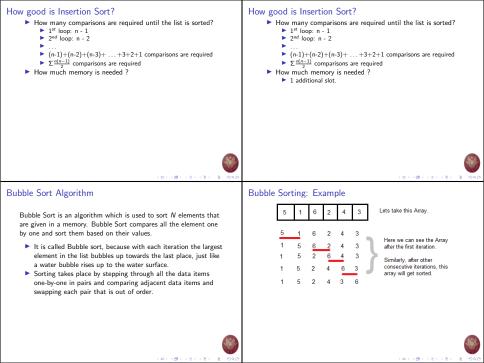
Original Array	After 1st pass	After 2nd pass	After 3rd pass	After 4th pass	After 5th pass
3	1	1	1	1	1
6	6	3	3	3	3
0	3 T	6	4	4	4
8	8	8	8	5	5
4	4	4	6	6	6
5	5	5	⑤ l	8	8

Selection Sort Code

```
a = [5, 1, 6, 2, 4, 3]
for i in range(0, len(a)):
    min = i
    for j in range(i + i, len(a) - 1):
        if a[j] > a[min]:
            min = j

temp = a[j]
    a[j] = a[min]
    a[min] = temp
```





Bubble Sort Code					
<pre>a = [5, 1, 6, 2, 4, 3] for i in range(0, len(a)): for j in range(0, len(a) - i - i): if a[j] > a[j+1]: temp = a[j] a[j] = a[j+1] a[j+1] = temp</pre>					
► The above algorithm is not efficient because a logic, the for-loop will keep executing for six in the list gets sorted after the second iteration.					
< => <					
How good is Bubble Sort? ► How many comparisons are required until the					

4 m > 4 # > 4 2 > 4 2 > 2 = 40 0 0

How good is Bubble Sort?

Bubble Sort Code: Version 2

iterations. a = [5, 1, 6, 2, 4, 3]for i in range(0, len(a)):

red until the list is sorted?

1011/01/12/12/12 2:00

How many comparisons are required until the list is sorted? ▶ 1st loop: n - 1 2nd loop: n - 2

 $\triangleright \sum \frac{n(n-1)}{2}$ comparisons are required

for j in range(0, len(a) - i - 1):

if a[j] > a[j+1]:

temp = a[i] a[i] = a[j+1]a[i+1] = temp

▶ We can insert a flag and can keep checking whether swapping of elements is taking place or not in the following iteration. If no swapping is taking place, it means the list is sorted and we can jump out of the for loop, instead executing all the

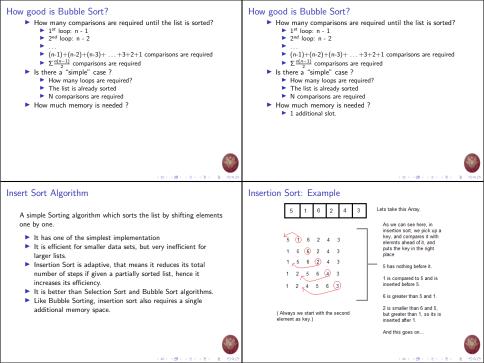
► (n-1)+(n-2)+(n-3)+ ...+3+2+1 comparisons are required

1011491121121 2 990

10110 10111 121 121 2 000

ent because as per the above iting for six iterations even if

How good is Bubble Sort? ► How many comparisons are required until the list is sorted? ► 1 st loop: n - 1 ► 2 nd loop: n - 2 ► ► (n-1)+(n-2)+(n-3)++3+2+1 comparisons are required ► ∑(n-1) comparisons are required ► Is there a "simple" case ?	How good is Bubble Sort? ► How many comparisons are required until the list is sorted? ► 1 st loop: n - 1 ► 2 nd loop: n - 2 ► ► (n-1)+(n-2)+(n-3)++3+2+1 comparisons are required ► Σ ^{n(m-1)} comparisons are required ► Is there a "simple" case ? ► How many loops are required?
How good is Bubble Sort? How many comparisons are required until the list is sorted? 1st loop: n - 1 2nd loop: n - 2 (n-1)+(n-2)+(n-3)++3+2+1 comparisons are required Example: case? How many loops are required? The list is already sorted	How good is Bubble Sort? How many comparisons are required until the list is sorted? 1st loop: n - 1 2st loop: n - 2 (n1)+(n-2)+(n-3)++3+2+1 comparisons are required External State a "simple" case? How many loops are required? The list is already sorted
	► N comparisons are required

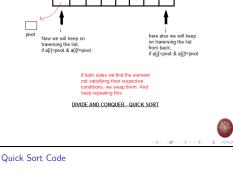


Insertion Sort Code a = [5, 1, 6, 2, 4, 3] for i in range(1, len(a)): key = a[i] j = i - 1 while j >= 0 and key < a[j]: a[j+1] = a[j] j - 1 a[j+2] = key key: we put each element of the list, in each pass, starting from the second element: a[1]. using the while loop, we iterate, until j becomes equal to zero or we find an element which is greater than key, and then we insert the key at that position.	How good is Insertion Sort? ► How many comparisons are required until the list is sorted?
10.10.12.13. 3 040	· D · (Ø · · 2 · · 3 · · 2 · ·) · 2 · · Ø
How good is Insertion Sort? ► How many comparisons are required until the list is sorted? ► 1 st loop: n - 1 ► 2 nd loop: n - 2 ► + 3+2+1 comparisons are required ► ∑ ⁿ⁽ⁿ⁻¹⁾ / ₂ comparisons are required	How good is Insertion Sort? ► How many comparisons are required until the list is sorted? ► 1* loop: n - 1 ► 2** loop: n - 2 ► (n-1)+(n-2)+(n-3)+ +3+2+1 comparisons are required ► \(\sum_{n=2}^{n-2}
(0) (0) (1) (2) (2) (2) (2)	101(0)(2)(2)(2)

How good is Insertion Sort? How many comparisons are required until the list is sorted? 1st loop: $n - 1$ 2nd loop: $n - 2$ $(n-1)+(n-2)+(n-3)++3+2+1$ comparisons are required $\sum \frac{n(n-1)}{2}$ comparisons are required $\sum \text{there a 'simple' case ?}$ The list is already sorted $N \text{ comparisons are required}$	How good is Insertion Sort? ► How many comparisons are required until the list is sorted? ► 1st loop: n - 1 ► 2nd loop: n - 2 ► ► (n-1)+(n-2)+(n-3)++3+2+1 comparisons are required ► 2 \frac{\sigma(n-2)}{2} \comparisons are required ► Is there a "simple" case? ► The list is already sorted ► N comparisons are required ► How much memory is needed?
How good is Insertion Sort? ► How many comparisons are required until the list is sorted? ► 1 st loop: n - 1 ► 2 nd loop: n - 2 ► ► (n-1)+(n-2)+(n-3)++3+2+1 comparisons are required	Quick Sort Algorithm Quick sort is very fast and requires very less additional space. It is based on the rule of Divide and Conquer. This algorithm divides the list into three main parts:
 ∑n(n-1) comparisons are required Is there a "simple" case ? The list is already sorted N comparisons are required How much memory is needed ? 1 additional slot. 	 ▶ Elements less than the Pivot element ▶ Pivot element(Central element) ▶ Elements greater than the pivot element ▶ Sorts any list very quickly ▶ Performance depends on the selection of the Pivot element
920 2 151121 920	10.00.00.00.00

List: 25 52 37 63 14 17 8 6 ▶ We pick 25 as the pivot. All the elements smaller to it on its left. All the elements larger than to its right. After the first pass the list looks like: 6 8 17 14 25 63 37 52 Now we sort two separate lists: 6.8.17.14 and 63.37.52 ▶ We apply the same logic, and we keep doing this until the complete list is sorted. 4 m > 4 m > 4 2 > 4 2 > 2 2 3 4 0 9 0 Quick Sort Code a = [25, 52, 37, 63, 14, 17, 8, 6] def partition(list, p, r): pivot = list[p]

Quick Sort: Example

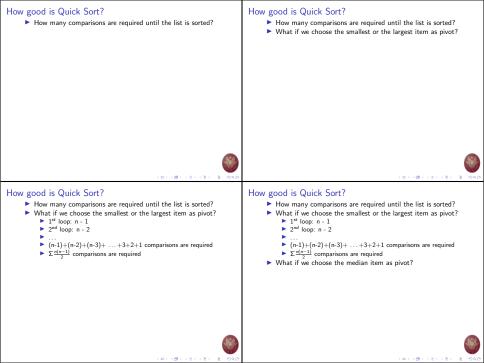


Quick Sort: Example

```
def quicksort(list, p, r):
                                                                              if (p < r):
                                                                                  q = partition(list, p, r)
                                                                                  quicksort(list, p, q);
i = p
                                                                                  quicksort(list, q + 1, r);
i = r
while(1):
                                                                          print("Before: ", a)
    while(list[i] < pivot and list[i] != pivot):
                                                                          quicksort(a, 0, len(a) - 1)
        i += 1
                                                                          print("After: ", a)
    while(list[j] > pivot and list[j] != pivot):
        i -= 1
    if(i < j):
        temp = list[i]
        list[i] = list[i]
        list[i] = temp
    else:
        return i
```

4 D > 4 B > 4 B > 4 B > 3 B + 4 9 0





How good is Quick Sort? How many comparisons are required until the list is sorted? What if we choose the smallest or the largest item as pivot? ▶ 1st loop: n - 1 2nd loop: n = 2 ▶ (n-1)+(n-2)+(n-3)+ ... +3+2+1 comparisons are required Σ n(n-1)/2 comparisons are required What if we choose the median item as pivot? 1st loop: two lists n each 2nd loop: four lists n each log n steps For each partition we do n comparisons In total n log n comparisons How many comparisons are required until the list is sorted?

How good is Quick Sort?

How many comparisons are required until the list is sorted? What if we choose the smallest or the largest item as pivot?

▶ 1st loop: n - 1 2nd loop: n = 2 (n-1)+(n-2)+(n-3)+ . . . +3+2+1 comparisons are required Σ n(n-1)/2 comparisons are required

▶ What if we choose the median item as pivot? 1st loop: two lists n each 2nd loop: four lists n each

log n steps For each partition we do n comparisons

In total n log n comparisons ▶ How much memory is needed ?



(B) (B) (E) (E) (E) (9)

How good is Quick Sort?

- ▶ What if we choose the smallest or the largest item as pivot? ▶ 1st loop: n - 1 ▶ 2nd loop: n - 2
 - ▶ (n-1)+(n-2)+(n-3)+ . . . +3+2+1 comparisons are required Σⁿ⁽ⁿ⁻¹⁾/₂ comparisons are required
 - What if we choose the median item as pivot? ▶ 1st loop: two lists ⁿ/₂ each
 - 2nd loop: four lists + each log n steps
 - For each partition we do n comparisons In total n log n comparisons
 - ► How much memory is needed ?
 - 1 additional slot.

2nd Assignment

https://www.hackerrank.com/

- Complete all Python challenges under the following subdomains:
- ► Complete 25 Algorithms challenges under the following subdomains:
 - Warmup (10), Sorting (any 10), Strings (any 5). You can cooperate, You can search on the Internet, ...
 - You need to write your own code
 - Email ichatz@diag.uniroma1.it
 - Subject: [PCS2] Homework 2 A .zip or a .tar.gz file with your python solutions, for all
 - challenges.





4 m > 4 d > 4 2 > 4 2 > 2 = 40 4 0