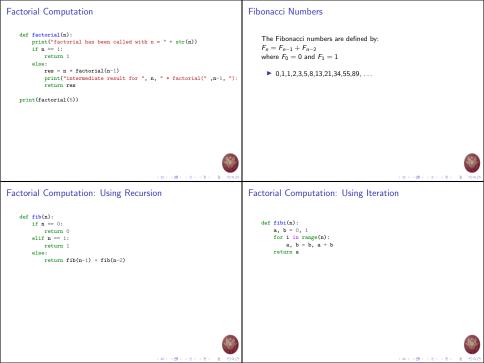
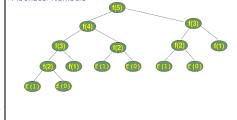
	Recursion Coding Style
Principles of Computer Science II Recursive Algorithms Ioannis Chatzigiannakis Sapienza University of Rome Lecture 6	Recursion is a way of programming or coding a problem, in which a function calls itself one or more times in its body. Usually, it is returning the return value of this function call. If a function definition fulfils the condition of recursion, we call this function a recursive function. Termination condition: A recursive function has to terminate to be used in a program. A recursive function terminates, if with every recursive call the solution of the problem is downsized and moves towards a base case. A base case is a case, where the problem can be solved without further recursion.
(0) (8) (8) (8)	(0) (0) (2) (2) (2) (2)
Factorial Computation: Using Iteration	Factorial Computation: Using Recursion
<pre>def iterative_factorial(n): result = 1 for i in range(2,n+i): result = : result = : return result</pre>	<pre>def factorial(n): if n == 1: return 1 else: return n * factorial(n-1)</pre>

т



Measure Performance from timeit import Timer from fibo import fib t1 = Timer("fib(10)","fr for i in range(1,41):

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Factorial Computation: Using Recursion and Memory

memo = {0:0, 1:1} def fibm(n): if not n in memo: memo(n) = fibm(n-1) + fibm(n-2) return memo(n)

In Merge Sort the unsorted list is divided into N sublists, each having one element, because a list consisting of one element is always sorted. Then, it repeatedly merges these sublists, to

Merge Sort Algorithm

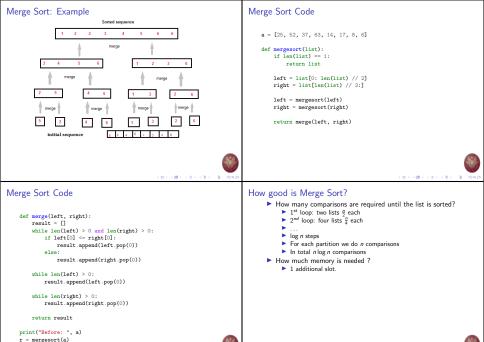
Fibonacci Numbers

produced.

Divide and Conquer algorithm
Performance always same for Worst, Average, Best case

renormance always same for worst, Average, best case

produce new sorted sublists, and in the end, only one sorted list is



1011/0011/01/05 05 090

4 D > 4 B > 4 B > 4 B > 3 B + 4 9 0

print("After: ", r)

Quick Sort Algorithm

Quick sort is very fast and requires very less additional space. It is based on the rule of Divide and Conquer. This algorithm divides the list into three main parts : Elements less than the Pivot element Pivot element(Central element)

Elements greater than the pivot element

 Sorts any list very quickly Performance depends on the selection of the Pivot element

4 m > 4 m > 4 2 > 4 2 > 2 2 3 4 0 9 0

4 D > 4 B > 4 B > 4 B > 3 B + 4 9 0



Quick Sort: Example List: 25 52 37 63 14 17 8 6

▶ We pick 25 as the pivot.

6 8 17 14 25 63 37 52

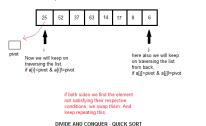
6.8.17.14 and 63.37.52

Now we sort two separate lists:

All the elements smaller to it on its left.

All the elements larger than to its right. After the first pass the list looks like:

Quick Sort: Example



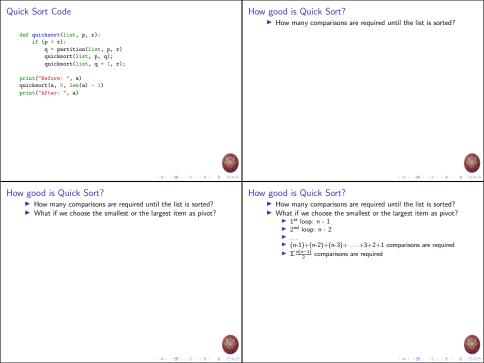
else: return i

Quick Sort Code

```
a = [25, 52, 37, 63, 14, 17, 8, 6]
def partition(list, p, r):
   pivot = list[p]
   i = p
   i = r
    while(1):
       while(list[i] < pivot and list[i] != pivot):
            i += 1
       while(list[j] > pivot and list[j] != pivot):
            i -= 1
        if(i < j):
            temp = list[i]
            list[i] = list[i]
            list[i] = temp
```

4 m x 4 m x 4 2 x 4 2 x 1 2 1 40 4 0

101 (8) (2) (2) (3) 3 (9)



How good is Quick Sort? ► How many comparisons are required until the list is sorted? ► What if we choose the smallest or the largest item as pivot? ► 1 st loop: n - 1 ► 2 nd loop: n - 2 ► (n-1)+(n-2)+(n-3)++3+2+1 comparisons are required ► ∑ ⁿ⁽ⁿ⁻¹⁾ / _n comparisons are required ► What if we choose the median item as pivot?	How good is Quick Sort? ► How many comparisons are required until the list is sorted? ► What if we choose the smallest or the largest item as pivot? ► 1 st loop: n - 1 ► 2 nd loop: n - 2 ► (n-1)+(n-2)+(n-3)+ +3+2+1 comparisons are required ► ∑ ⁿ⁽ⁿ⁻¹⁾ / _{n(n-1)} comparisons are required ► What if we choose the median item as pivot? ► 1 st loop: two lists ^g / _n each ► 2 nd loop: four lists ^g / _n each ► ► log n steps ► For each partition we do n comparisons ► In total n log n comparisons
· □ · · Ø · · 8 · · 8 · · 8 · · 9 · 0	101001200200000000000000000000000000000
How good is Quick Sort? ► How many comparisons are required until the list is sorted? ► What if we choose the smallest or the largest item as pivot? ► 1 st loop: n - 2 ► (n-1) + (n-2) + (n-3) + + 3 + 2 + 1 comparisons are required ► ∑ ^{n(g-1)} / _{n(g-1)} comparisons are required ► What if we choose the median item as pivot? ► 1 st loop: two lists ½ each ► 2 nd loop: four lists ½ each ► ► log n steps ► For each partition we do n comparisons ► In total n log n comparisons ► How much memory is needed?	How good is Quick Sort? ► How many comparisons are required until the list is sorted? ► What if we choose the smallest or the largest item as pivot? ► 1 st loop: n - 1 ► 2 nd loop: n - 2 ► (n-1)+(n-2)+(n-3)+ +3+2+1 comparisons are required ► ∑ ⁿ⁽⁻¹⁾ / _{n-2} comparisons are required ► What if we choose the median item as pivot? ► 1 st loop: two lists ½ each ► 2 nd loop: four lists ½ each ► ► log n steps ► For each partition we do n comparisons ► In total n log n comparisons ► How much memory is needed? ► 1 additional slot.
(D) (B) (E) (E) E OQC	(D) (Ø) (2) (2) 2 OQC