Principles of Computer Science II Sequence Similarity

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Lecture 6



Generalized Equivalent Words

Find an algorithm to solve a generalization of the Equivalent Words problem when insertions, deletions, and substitutions are allowed (rather than only substitutions).

- Given two words v, w and a dictionary, find out whether the words are equivalent.
- Your program should output the series of transformations for v to become w
- Use the following dictionary: https://goo.gl/hBvqqr
- Example: To transform head into tea one can use four intermediates:

 $\mathsf{head} \to \mathsf{heal} \to \mathsf{teal} \to \mathsf{tea}$

Equivalent Words

Transform one English word v into another word w by going through a series of intermediate English words, where each word in the sequence differs from the next by only one substitution (1 character).

- Given two words v, w and a dictionary, find out whether the words are equivalent.
- Your program should output the series of transformations for v to become w
- Use the following dictionary: https://goo.gl/hBvqqr

Example: To transform head into tail one can use four intermediates: head → heal → teal → tell → tall → tail



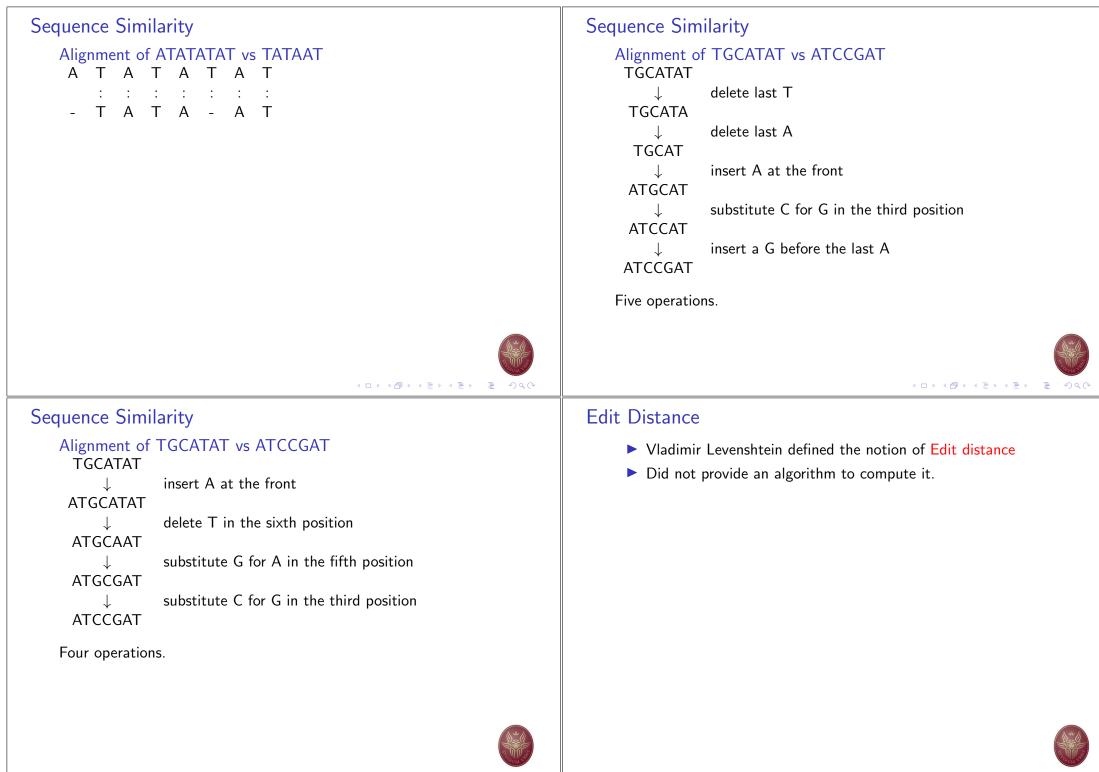
Edit Distance

- ▶ We looked for repeating patterns within DNA sequences.
- How can we measure the similarity between different sequences?
- ▶ We use the notion of Vladimir Levenshtein introduced in 1966
- Edit distance the minimum number of editing operations needed to transform one string into another (insert/delete symbol or substitute one symbol for another).

Alignment of ATATATAT vs TATATATA

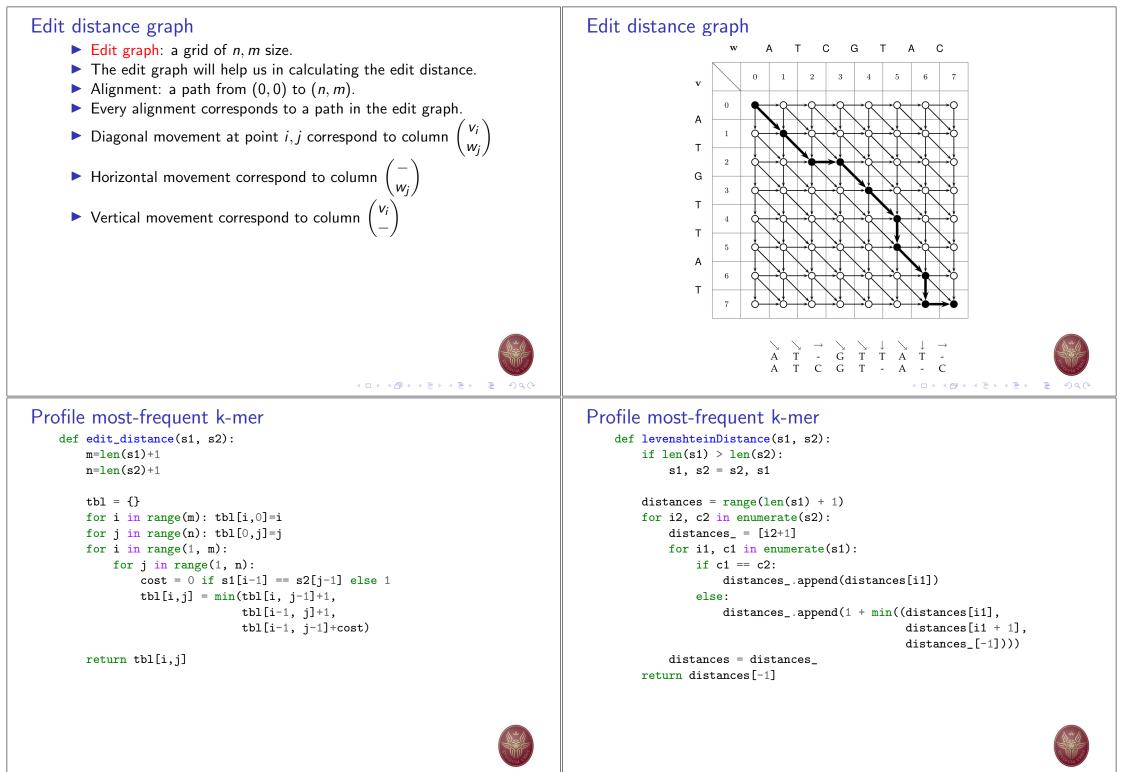
А	Т	А	Т	А	Т	А	Т	-
	:	:	:	:	:	:	:	
-	Т	А	Т	А	Т	А	Т	А





 Edit Distance Algorithm using Dynamic Programming Assume two strings: v (of n characters) w (of m characters) The alignment of v, w is a two-row matrix such that first row: contains the characters of v (in order) second row: contains the characters of w (in order) spaces are interpersed throughout the table. Characters in each string appear in order, though not necessarily adjacently. 	Edit Distance Algorithm using Dynamic Programming A T - G T T A T - A A T C G T - A - C • Matches – columns with the same letter, • Mismatches – columns with different letters. • Model on the same letter, • • Columns containing one space are called indels • Space on top row: insertions • Space on bottom row: deletions # matches + # mismatches + # indels < n + m
 No column contains spaces in both rows. At most n + m columns. 	
 Representing the rows v A T - G T T A T - w A T C G T - A - C One way to represent v AT-CGTAT- One way to represent w ATCGT-A-C Another way to represent v AT-CGTAT- Another way to represent v AT-CGTAT- I22345677 number of symbols of v present up to a given position Similarly, to represent w ATCGT-A-C 123455667 	Representing the rows $ \begin{array}{c} \hline \mathbf{v} & \underline{A} & \underline{T} & \underline{-} & \underline{G} & \underline{T} & \underline{T} & \underline{A} & \underline{T} & \underline{-} \\ \hline \mathbf{w} & \underline{A} & \underline{T} & \underline{C} & \underline{G} & \underline{T} & \underline{-} & \underline{A} & \underline{-} & \underline{C} \\ \hline \hline \mathbf{w} & \underline{A} & \underline{T} & \underline{C} & \underline{G} & \underline{T} & \underline{-} & \underline{A} & \underline{-} & \underline{C} \\ \hline \hline \mathbf{w} & \underline{1} & \underline{2} & \underline{2} & \underline{3} & \underline{4} & \underline{5} & \underline{6} & \underline{7} & \underline{7} \\ \hline \mathbf{w} & \underline{1} & \underline{2} & \underline{3} & \underline{4} & \underline{5} & \underline{5} & \underline{6} & \underline{6} & \underline{7} \\ \hline \mathbf{w} & \underline{1} & \underline{2} & \underline{3} & \underline{4} & \underline{5} & \underline{5} & \underline{6} & \underline{6} & \underline{7} \\ \hline \mathbf{w} & \underline{1} & \underline{2} & \underline{3} & \underline{4} & \underline{5} & \underline{5} & \underline{6} & \underline{6} & \underline{7} \\ \hline \mathbf{w} & \underline{1} & \underline{2} & \underline{2} & \underline{3} & \underline{4} & \underline{5} & \underline{5} & \underline{6} & \underline{6} & \underline{7} \\ \hline 0 & \begin{pmatrix} 1 \\ 1 \end{pmatrix} & \begin{pmatrix} 2 \\ 2 \end{pmatrix} & \begin{pmatrix} 2 \\ 3 \end{pmatrix} & \begin{pmatrix} 3 \\ 4 \end{pmatrix} & \begin{pmatrix} 4 \\ 5 \end{pmatrix} & \begin{pmatrix} 5 \\ 5 \end{pmatrix} & \begin{pmatrix} 6 \\ 6 \end{pmatrix} & \begin{pmatrix} 7 \\ 6 \end{pmatrix} & \begin{pmatrix} 7 \\ 6 \end{pmatrix} & \begin{pmatrix} 7 \\ 7 \end{pmatrix} \\ \hline \end{array} \\ \hline \end{array} $ The entire alignment is simply a path: $(0,0) \rightarrow (1,1) \rightarrow (2,2) \rightarrow (2,3) \rightarrow (3,4) \rightarrow (4,5) \rightarrow (5,5) \rightarrow (6,6) \rightarrow (7,6) \rightarrow (7,7) \\\hline \end{array} $

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2nd Assignment https://www.hackerrank.com/

- Complete a total of 25 Python challenges from the following subdomains:
 - Algorithms: Warmup (10), Sorting (any 10), Strings (any 5)
- ▶ You can cooperate, You can search on the Internet, ...
- You need to write your own code
- Email ichatz@diag.uniroma1.it Subject: [PCS2] Homework 2 Your GitHub repository with your solutions, for all challenges. Also send your hackerrank user account link: https://www.hackerrank.com/{username}

Deadline: 7 November 2022

